

Motivation

Angular distributions of differential cross sections and other polarization observables from the latest CLAS data sets, for reaction $\gamma + p \rightarrow K^+ + \Lambda$ have been analysed using Legendre Polynomials.

In this work, we try to establish the most important baryon resonances which contribute to the $p(\gamma, K^+) \Lambda$ reaction. All observables can be represented by Legendre polynomial series (see Figure.1), where the Legendre coefficients may reflect qualitatively the baryon resonances structure. In addition, extracting Legendre coefficients may thus describe features of different resonances more directly than angular distributions alone.

One of the main questions to be addressed in this work is how many Legendre polynomials are required to describe the data. We construct data models with different number of Legendre polynomial components have been compared by calculating posterior probabilities in light of the data.

$$\begin{aligned} \mathcal{L}_0(I, \vec{E}, \vec{C}_{z'}, \vec{L}_{z'}) &\rightarrow \sum_l \dots P_{l0}(x), \\ \mathcal{L}_1 a(\vec{P}, \vec{H}, \vec{C}_{z'}, \vec{L}_{z'}) &\rightarrow \sum_l \dots P_{l1}(x), \\ \mathcal{L}_1 b(\vec{T}, \vec{F}, \vec{O}_{z'}, \vec{T}_{z'}) &\rightarrow \sum_l \dots P_{l1}(x), \\ \mathcal{L}_2(\vec{\Sigma}, \vec{G}, \vec{O}_{z'}, \vec{T}_{z'}) &\rightarrow \sum_l \dots P_{l2}(x). \end{aligned}$$

Figure 1: All observables represented by Legendre Polynomials

According to reaction channel in Figure. 4 we can calculate the sixteen observables in helicity representation and can classified them into four Legendre polynomials.

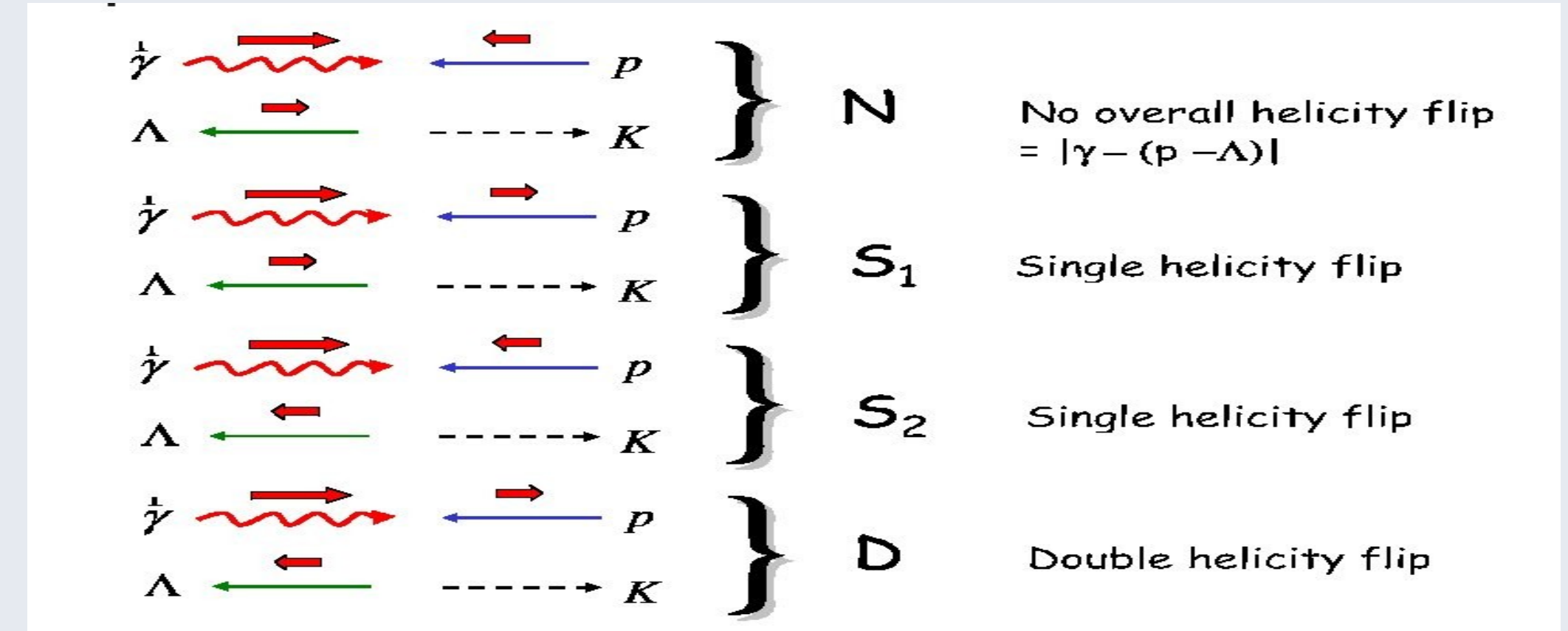


Figure 5: Helicity Representation

Analysis Procedure

We constructed data model :

Data Model

$$M_0 = A_0 P_0(\cos \theta)$$

$$M_1 = M_0 + A_1 P_1(\cos \theta).$$

$$M_l = M_0 + M_1 + \dots + A_l P_l(\cos \theta)$$

Model comparison

$$R = \frac{P(M_i|D)}{P(M_0|D)} = \frac{P(D|M_i)P(M_i)}{P(D|M_0)P(M_0)}$$

Marginalisation Likelihood

$$P(D|M_i) = \int \dots \int P(D, A_0, A_1, \dots, A_l | M_i) dA_0 dA_1 \dots dA_l$$

$$P(D, A_0, A_1, \dots, A_l | M_i) = P(D | A_0, A_1, \dots, A_l, M_i) \times P(A_0, A_1, \dots, A_l | M_i)$$

$$P(D | A_0, A_1, \dots, A_l, M_i) \propto \exp\left(-\frac{\chi^2}{2}\right)$$

K Λ Reaction Channel

How do we choose this reaction?

Constituent quark model (CQM) predict a much richer baryon resonances spectrum than has been observed in the experiments [S. Capstick & Roberts, PRD58(1998)074011]. These missing resonances may couple strongly to K Λ and K Σ channels. So this channel appears as best solution to search baryon resonances.

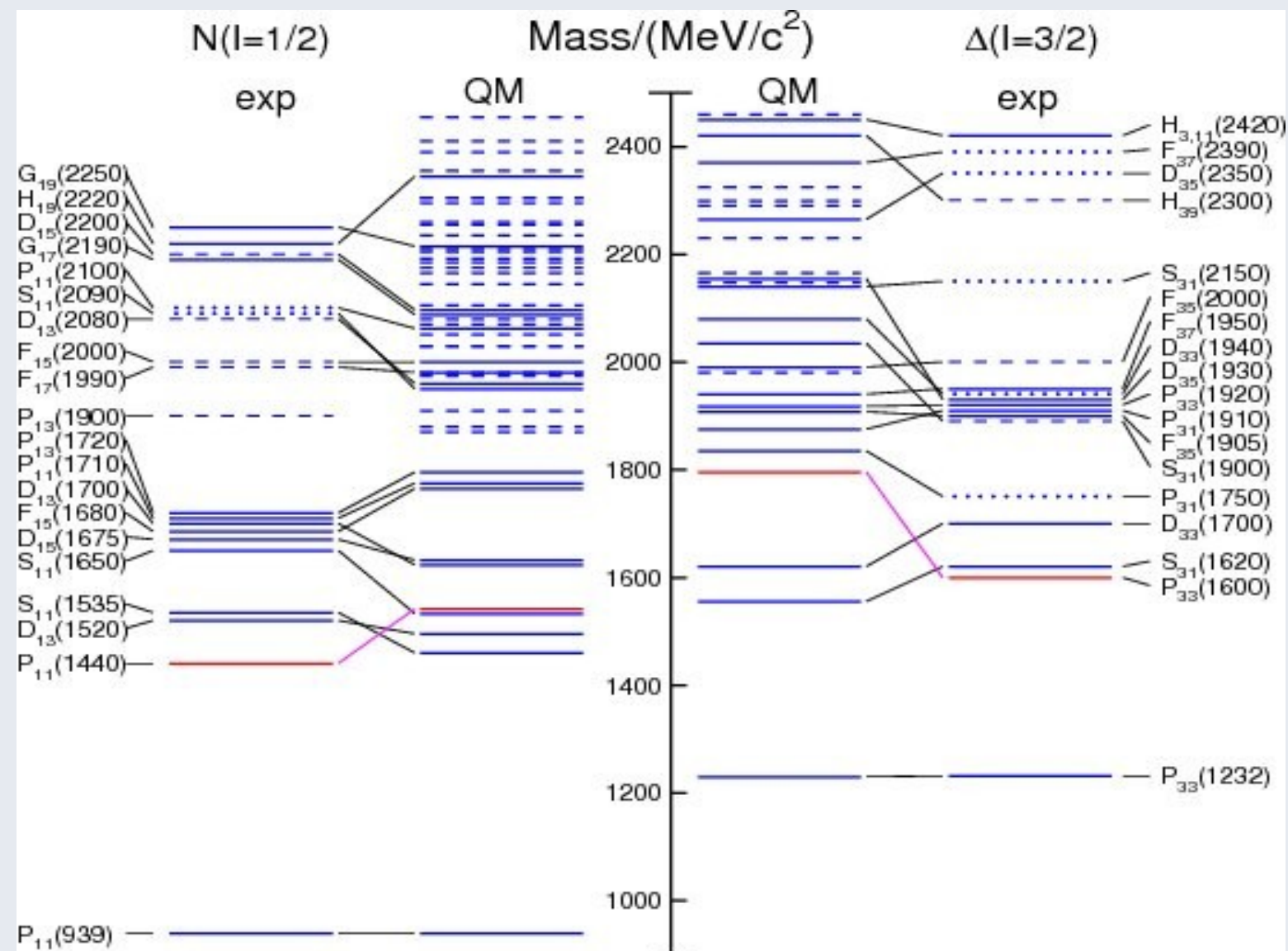


Figure 2: Baryon Resonances Spectrum

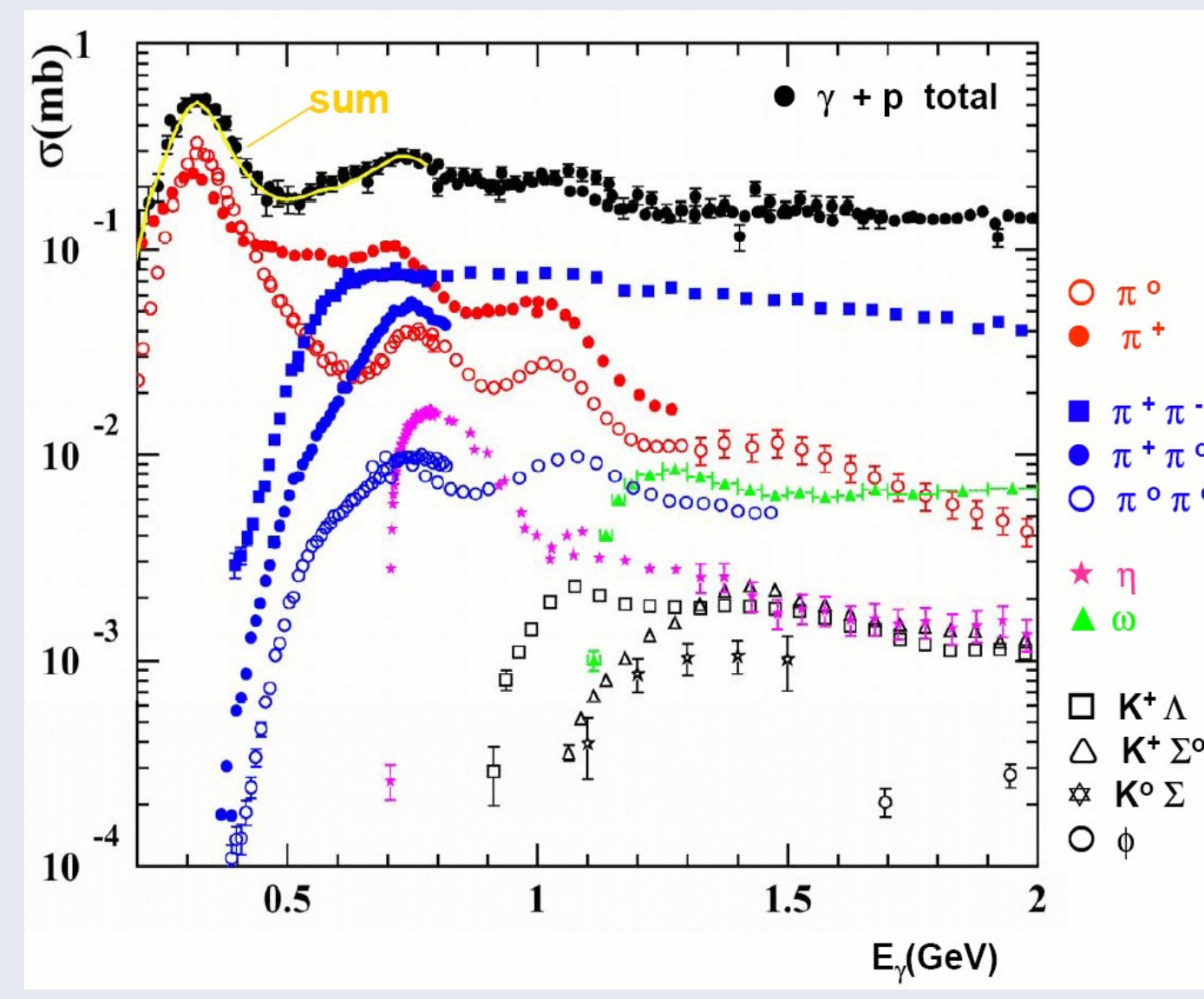


Figure 3: Kaon Photoproduction contribution on the proton

How do we study baryon resonances?

From the reaction channel in Figure. 4, we can calculate all observables using helicity representation.

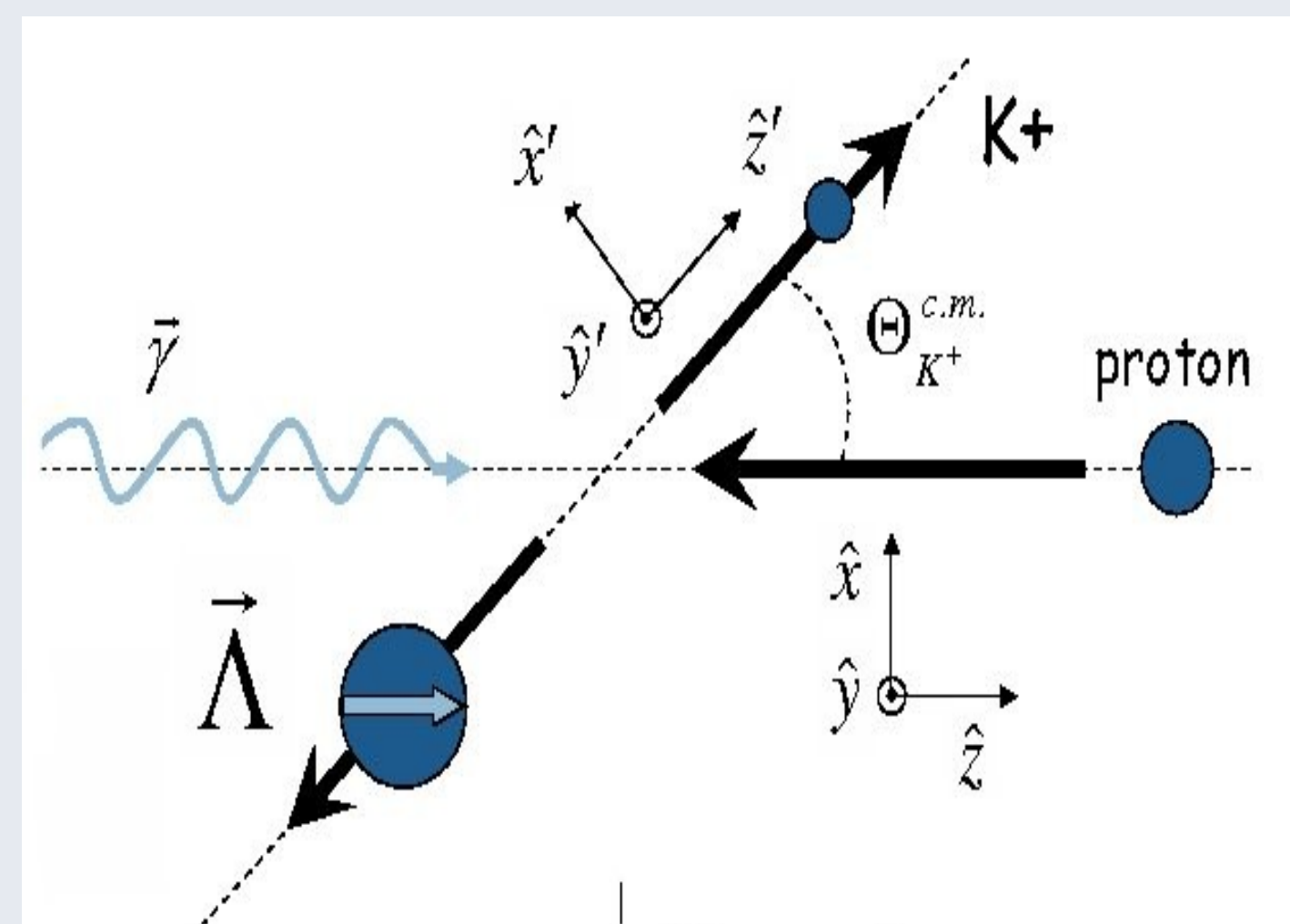


Figure 4: Reaction channel for $\gamma + p \rightarrow K^+ + \Lambda$

Double and single observables

- Differential cross section ($d\sigma/d\Omega$)
- Single polarization (P, Σ , T)
- Beam Target polarization (E, F, G, H)
- Beam-Recoil polarization (C_z, C_x, O_z, O_x)
- Target-Recoil polarization (T_x, T_z, L_x, L_z)

Preliminary Results

Differential Cross Section (photon energy = 1.824 GeV)

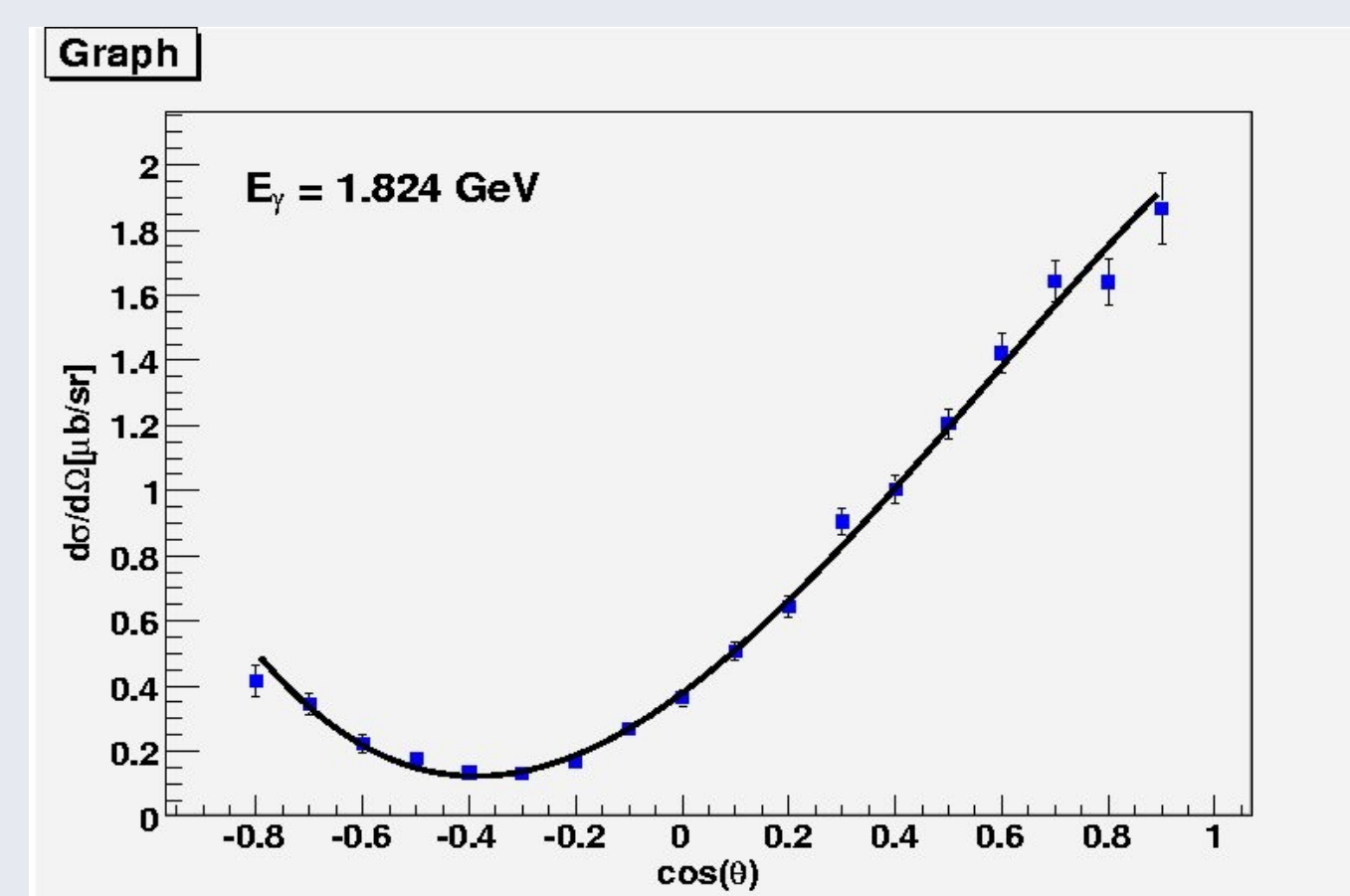


Figure 6: LP predicted results

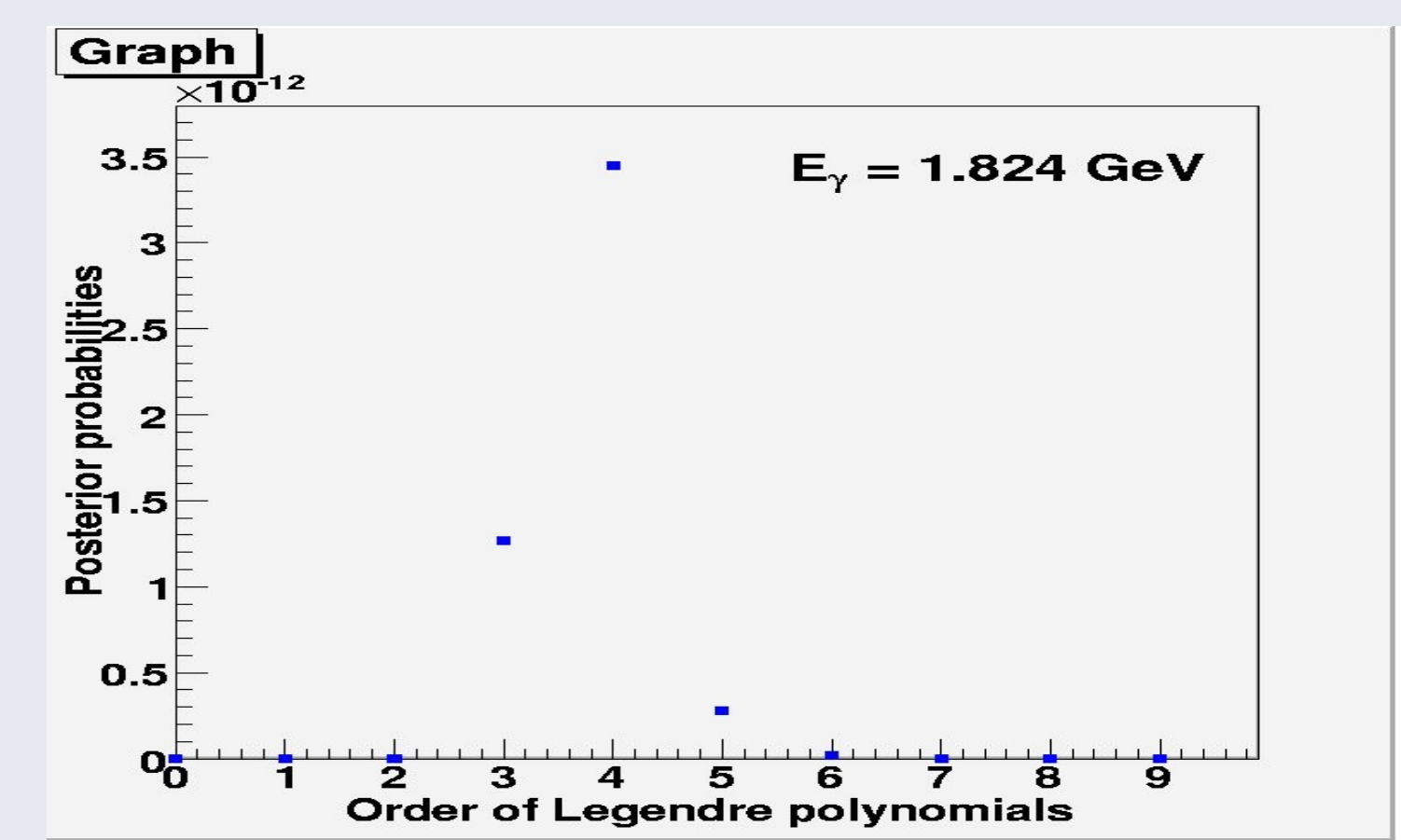


Figure 7: The maximum posterior

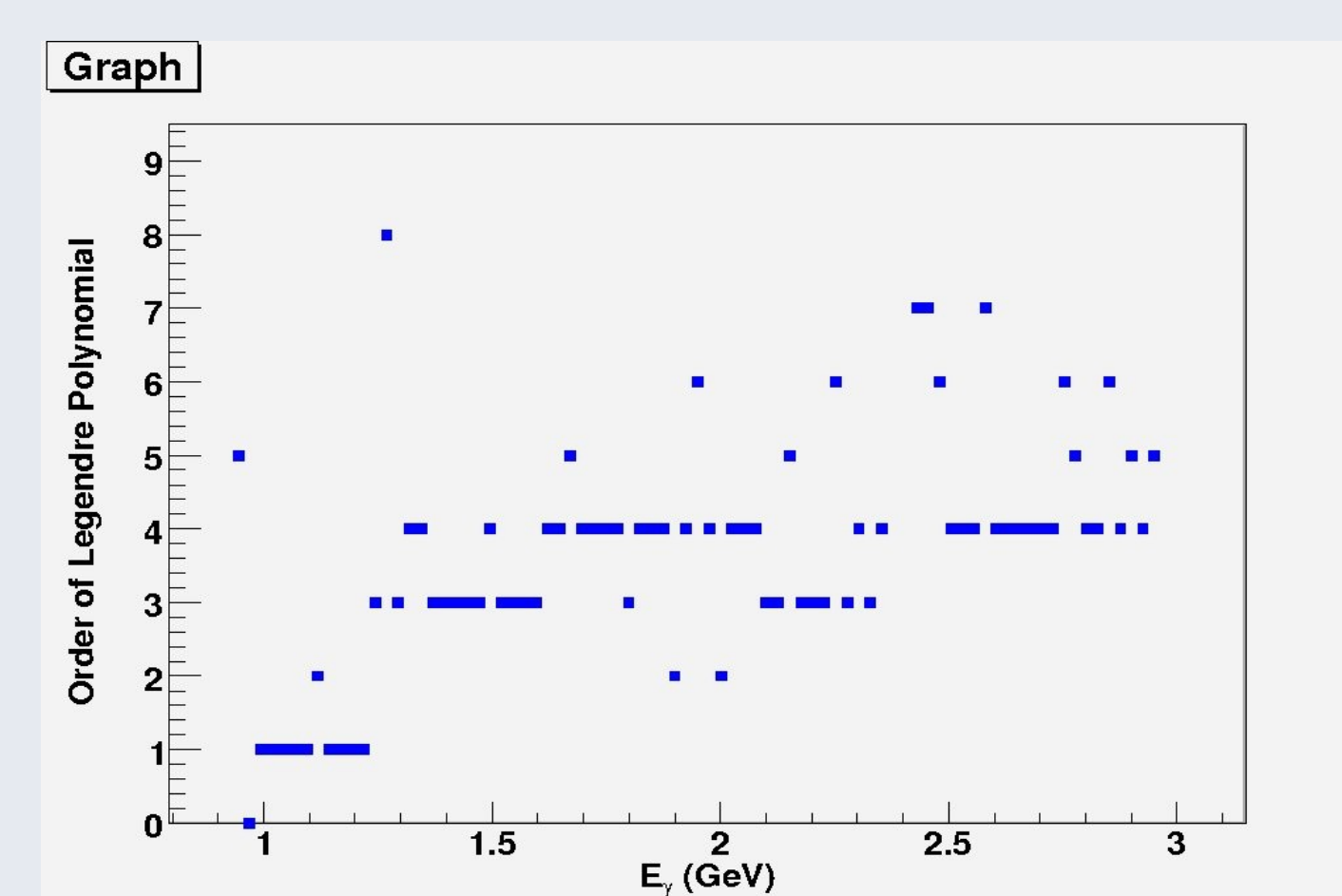


Figure 8: order of LP vs photon energy

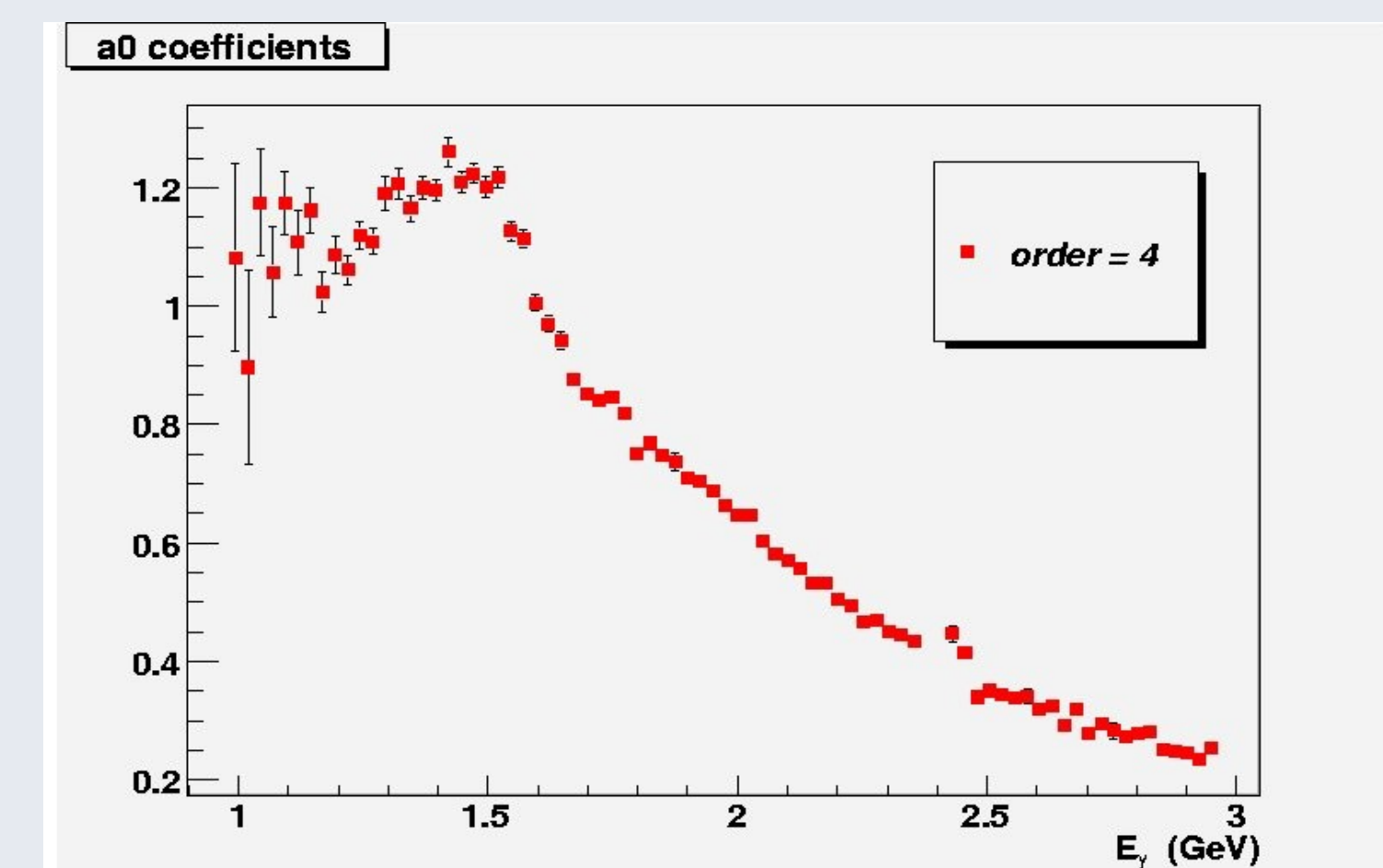


Figure 9: LP Coefficient extracted

