

# Pion photoproduction in a dynamical coupled-channels model

Fei Huang

Department of Physics and Astronomy, The University of Georgia, USA

Collaborators:

K. Nakayama (UGA), H. Haberzettl (GWU)

M. Döring, Ulf-G. Meißner (Bonn U.)

J. Haidenbauer, C. Hanhart, S. Krewald (FZ-Jülich)

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- Introduction
- Jülich  $\pi N$  dynamical coupled-channels model
  - Dynamical model ingredients
  - $\pi N$  partial wave amplitudes from Jülich model
- $\pi$  photoproduction
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  - Multipole amplitudes & target asymmetries
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# Methodology for $N^*$ study

complete set of data for  $\gamma N \rightarrow KY$



There are lots of high precision data from JLab, MIT-Bates, BNL-LEGS, Mainz-MAMI, Bonn-ELSA, GRAAL, Spring-8, et al.

$N^*$ 's are unstable and couple strongly to baryon-meson states



Build coupled-channels meson-baryon reaction models to

- analyze the meson production data
- extract  $N^*$  parameters
- understand the reaction mechanisms
- understand the structures and dynamical origins of  $N^*$

Most widely used models: K matrix approximation, chiral unitary approach, dynamical coupled-channels model, et al.



# Dynamical model ingredients

$$T = \text{[Diagram: loop with two vertices and two external lines]} + X$$

(a)

$$T = V + \text{[Diagram: loop with V and T vertices and two external lines]}$$

(b)

$$X = U + \text{[Diagram: loop with U and X vertices and two external lines]}$$

(d)

$$V = \text{[Diagram: bare vertex with two external lines]} + U$$

(c)

$$U = \text{[Diagram: loop with two vertices and two external lines]} + \dots$$

(e)

(a)  $T = |F\rangle S \langle F| + X$

$T$ : full amplitude

$S$ : dressed res. propagator

(b)  $T = V + V G_0 T$

$X$ : non-pole amplitude

$S_0$ : bare res. propagator

(c)  $V = |f\rangle S_0 \langle f| + U$

$U$ : driving term of  $X$

$|F\rangle$ : dressed res. vertex

(d)  $X = U + U G_0 X$

$V$ : driving term of  $T$

$|f\rangle$ : bare res. vertex

$$S = S_0 + \text{[Diagram: self-energy loop on a propagator]}$$

(a)

(a)  $S = S_0 + S \underbrace{\langle F| G_0 |f\rangle}_{\text{"self energy"} \Sigma} S_0$

"self energy"  $\Sigma$

$$|F\rangle = |f\rangle + \text{[Diagram: loop with X and |f> vertices and two external lines]}$$

(b)

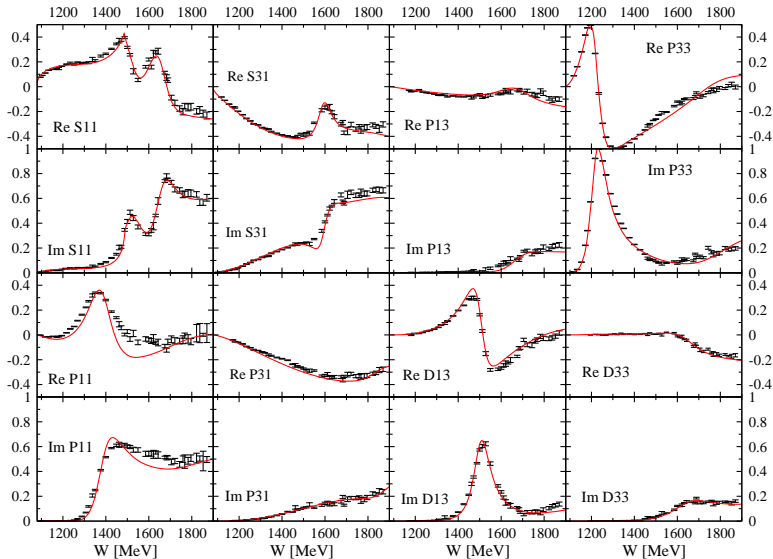
(b)  $|F\rangle = |f\rangle + X G_0 |f\rangle$



# Jülich model: $\pi N \rightarrow \pi N$ [Solution 2002]

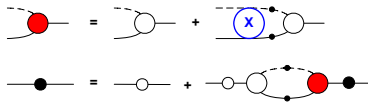
$$\pi N \oplus \eta N \oplus \pi \Delta \oplus \rho N \oplus \sigma N$$

$S_{11}(1535)$ ,  $S_{11}(1650)$ ,  $S_{31}(1620)$ ,  $P_{31}(1910)$ ,  $P_{13}(1720)$ ,  $D_{13}(1520)$ ,  $P_{33}(1232)$ ,  $D_{33}(1700)$  (all are 4-star  $N^*$ 's)

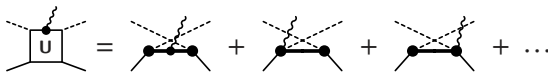
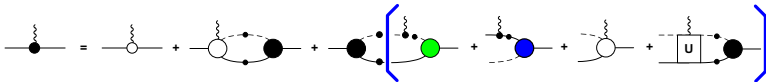
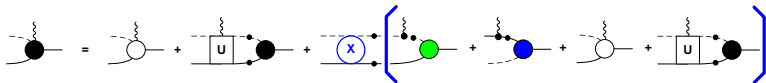


# Pion photoproduction [H. Haberzettl, PRC56(1997)2041]

To get  $M^\mu$  &  $J^\mu$ , attach a photon everywhere to

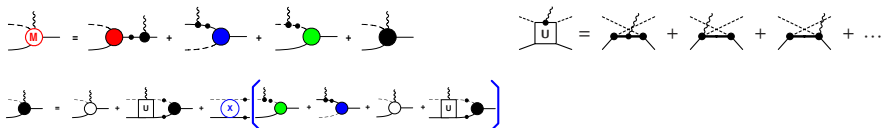


$$\begin{array}{c}
 \text{Diagram: } M^\mu \\
 M^\mu = M_s^\mu + M_u^\mu + M_t^\mu + M_{\text{int}}^\mu
 \end{array}$$



# Gauge invariance

- In a full theory (no form factors & truncations), gauge invariance is respected (minimum coupling,  $\partial_\mu \rightarrow D_\mu \equiv \partial_\mu + ieA_\mu(x)$ )
- Real-world calculations require form factors & truncations



- Inclusion form factors will destroy gauge invariance, since form factors are usually functions of the momenta of exchanged particles
- Truncations usually also destroy gauge invariance
- **The vast majority of existing models does not satisfy gauge invariance**
- **Our model is gauge invariant**  $\leftarrow$  we introduce a prescription to restore gauge invariance

# Prescription to restore gauge invariance

The diagram shows a vertex  $M$  (represented by a red circle with a wavy line) equal to the sum of four terms:  $M_s^\mu$  (red circle with a dashed line),  $M_u^\mu$  (blue circle with a dashed line),  $M_t^\mu$  (green circle with a dashed line), and  $M_{int}^\mu$  (black circle with a dashed line).

$$M^\mu = M_s^\mu + M_u^\mu + M_t^\mu + M_{int}^\mu$$

The diagram shows a vertex  $M_c$  (black circle with a wavy line) equal to the sum of several terms: a white circle with a wavy line, a box labeled  $U$  with a dashed line, a circle labeled  $X$  with a dashed line, and a group of terms in brackets: a green circle with a dashed line, a blue circle with a dashed line, a white circle with a wavy line, and a box labeled  $U$  with a dashed line.

$$M_c^\mu \equiv m_{KR}^\mu + U^\mu G_0 |F\rangle + X G_0 (M_u^\mu + M_t^\mu + m_{KR}^\mu + U^\mu G_0 |F\rangle)_L$$

$$M_{int}^\mu = M_c^\mu + X G_0 (M_u^\mu + M_t^\mu + M_c^\mu)_T$$

## Generalized Ward-Takahashi Identity (GWTI) for $M^\mu$

$$k_\mu M^\mu = - |F_s \tau\rangle S_{p+k} Q_i S_p^{-1} + S_{p'}^{-1} Q_f S_{p'-k} |F_u \tau\rangle + \Delta_{p-p'+k}^{-1} Q_\pi \Delta_{p-p'} |F_t \tau\rangle$$



## Constraints on $M_c^\mu$ & $M_{int}^\mu$

$$k_\mu M_c^\mu \equiv k_\mu M_{int}^\mu = - |F_s \tau\rangle Q_i + Q_f |F_u \tau\rangle + Q_\pi |F_t \tau\rangle$$



# Choosing the generalized contact current $M_c^\mu$

- Constraints: gauge invariance; contact term; crossing symmetry
- Choosing the generalized contact current  $M_c^\mu$  as

$$M_c^\mu = -g_\pi \gamma_5 \left\{ \left[ \lambda + (1 - \lambda) \frac{\not{q}}{2m} \right] C^\mu + (1 - \lambda) \frac{\gamma^\mu}{2m} e_\pi f_t \right\}$$
$$C^\mu = e_\pi \frac{(2q - k)^\mu}{t - q^2} (f_t - \hat{F}) + e_f \frac{(2p' - k)^\mu}{u - p'^2} (f_u - \hat{F}) + e_i \frac{(2p + k)^\mu}{s - p^2} (f_s - \hat{F})$$
$$\hat{F} = 1 - \hat{h} (1 - \delta_s f_s) (1 - \delta_u f_u) (1 - \delta_t f_t)$$

$k, p, q, p'$ : 4-momenta for incoming  $\gamma$ ,  $N$  & outgoing  $\pi$ ,  $N$

$\hat{h}$ : fit parameter

$f_x$ : form factors for corresponding channels

- Check gauge invariance:

$$k_\mu M_c^\mu = -|F_s\rangle e_i + |F_u\rangle e_f + |F_t\rangle e_\pi$$

- If no form factors, i.e.  $f_x = 1$ ,

$$C^\mu \rightarrow 0, \quad M_c^\mu \rightarrow -g_\pi \gamma_5 (1 - \lambda) \frac{\gamma^\mu}{2m} e_\pi \quad (\text{Kroll-Ruderman term})$$

# Application

$$\text{M} = \text{contact} + \text{B} + \text{X} G_0 \text{B}_T \quad (\text{a})$$

$$M^\mu = |F\rangle S J^\mu + B^\mu + X G_0 B_T^\mu$$

$$\text{M} = \text{contact} + \text{B} + \text{T} G_0 \text{B}_T \quad (\text{b})$$

$$M^\mu = |F\rangle S \tilde{J}_s^\mu + B^\mu + T G_0 B_T^\mu$$

$$\text{B} = \text{contact} + \text{meson exchange} + \text{contact} \quad (\text{c})$$

$$B^\mu = M_u^\mu + M_t^\mu + M_c^\mu$$

$$\text{quark} = \text{contact} + \text{T} + \text{T} \quad (\text{a})$$

$$J^\mu = \tilde{J}_s^\mu + \langle F | G_0 B_T^\mu$$

$$\text{quark} = \text{contact} + \text{L} + \text{L} + \text{L} \quad (\text{b})$$

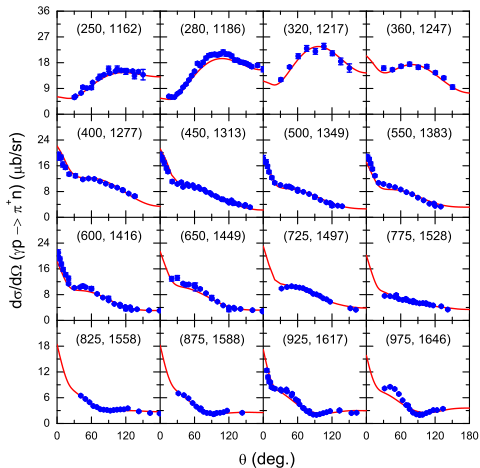
$$\tilde{J}_s^\mu = J_0^\mu + \langle m_{KR}^\mu | G_0 | F \rangle + \langle f | G_0 B_L^\mu$$

$\tilde{J}_s^\mu$ : minimal current. For more details, see:

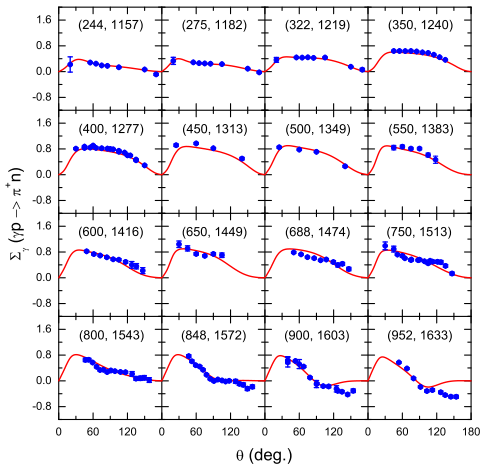
H. Haberzettl, F. Huang, and K. Nakayama, arXiv:1103.2065



# Results: $d\sigma/d\Omega$ & $\Sigma_\gamma$ for $\gamma + p \rightarrow \pi^+ + n$



Differential cross sections for  $\gamma + p \rightarrow \pi^+ + n$

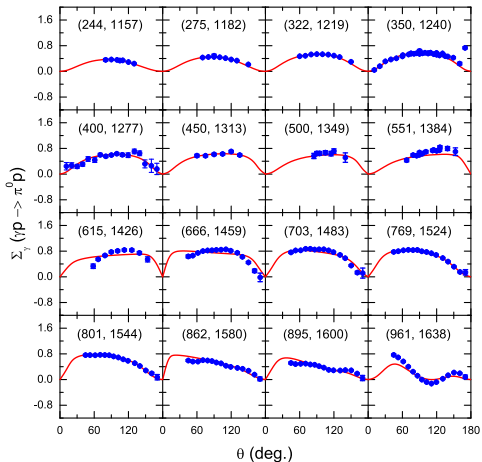
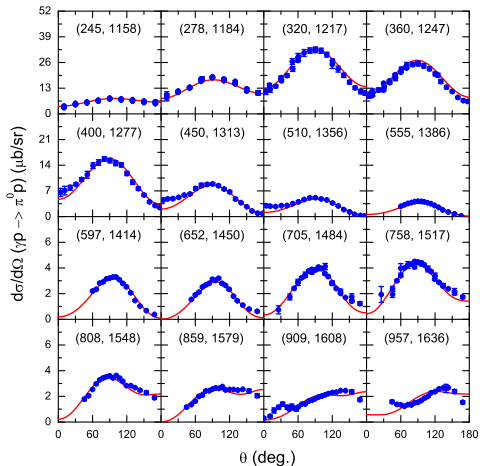


Photon spin asymmetries for  $\gamma + p \rightarrow \pi^+ + n$

$S_{11}(1535), S_{11}(1650), S_{31}(1620), P_{31}(1910), P_{13}(1720), D_{13}(1520), P_{33}(1232), D_{33}(1700)$



# Results: $d\sigma/d\Omega$ & $\Sigma_\gamma$ for $\gamma + p \rightarrow \pi^0 + p$



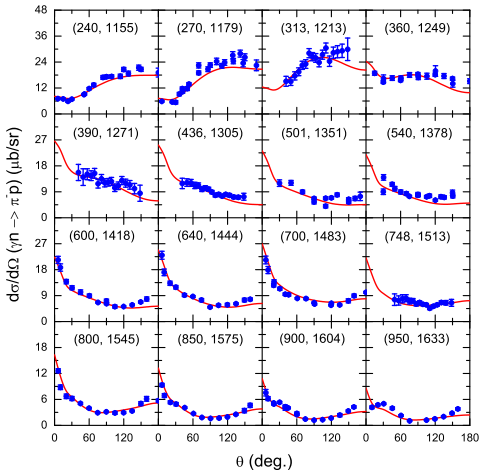
Differential cross sections for  $\gamma + p \rightarrow \pi^0 + p$

Photon spin asymmetries for  $\gamma + p \rightarrow \pi^0 + p$

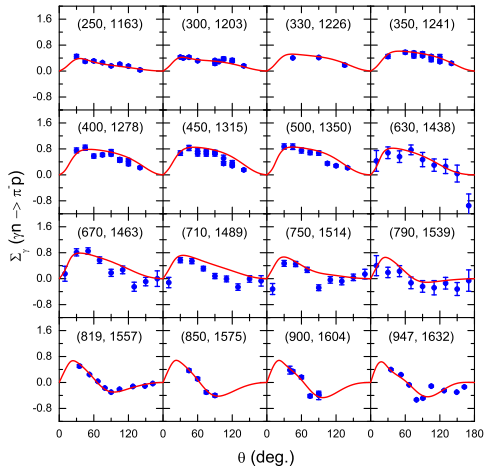
$S_{11}(1535), S_{11}(1650), S_{31}(1620), P_{31}(1910), P_{13}(1720), D_{13}(1520), P_{33}(1232), D_{33}(1700)$



# Results: $d\sigma/d\Omega$ & $\Sigma_\gamma$ for $\gamma + n \rightarrow \pi^- + p$



Differential cross sections for  $\gamma + n \rightarrow \pi^- + p$

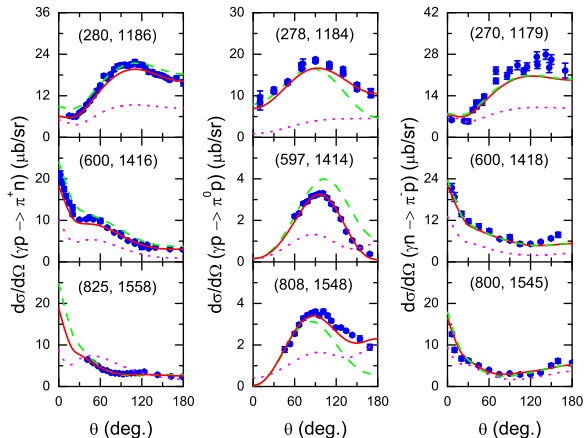


Photon spin asymmetries for  $\gamma + n \rightarrow \pi^- + p$

$S_{11}(1535), S_{11}(1650), S_{31}(1620), P_{31}(1910), P_{13}(1720), D_{13}(1520), P_{33}(1232), D_{33}(1700)$



# Contributions from loop integral & $M_c^\mu$

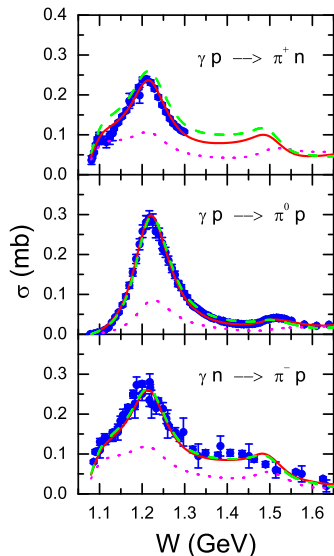


$$M^\mu = |F\rangle S \tilde{J}_s^\mu + M_u^\mu + M_t^\mu + M_c^\mu + T G_0 (M_u^\mu + M_t^\mu + M_c^\mu)_T$$

- : full calculation
- ⋯: no loop integral
- - -: no  $M_c^\mu$  apart from K.R.

- Contribution from the loop integral is important
- The terms apart from the Kroll-Ruderman term in  $M_c^\mu$  give significant effects  
⇒ keeping gauge invariance is important

# $\gamma N \rightarrow \pi N$ total cross sections

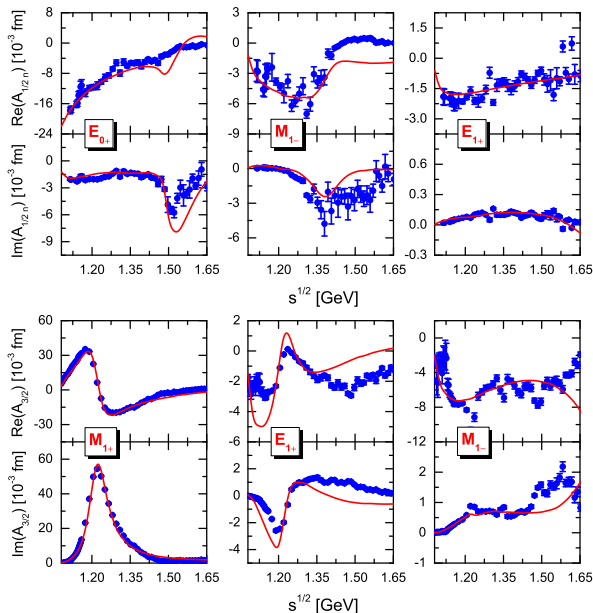


- : full calculation
- ⋯: no loop integral
- - -: no  $M_c^\mu$  apart from Kroll-Ruderman term

- Data not included in the fit
- Contribution from the loop integral is important
- Effect of the terms apart from Kroll-Ruderman term in  $M_c^\mu$  is significant for  $\gamma p \rightarrow \pi^+ n$
- For  $\gamma p \rightarrow \pi^0 p$ , the effect of  $M_c^\mu$  on  $d\sigma/d\omega$  is largely suppressed at backward angles by  $\sin \theta$



# Multipole amplitudes



- SAID's PWA not included in the fit

- $I = 1/2$ :

$E_{0+}$ :  $S_{11}(1535)$ ,  $S_{11}(1650)$

$M_{1-}$ :  $P_{11}(1440)$

$E_{1+}$ :  $P_{13}(1720)$

- $I = 3/2$ :

$M_{1+}$ :  $P_{33}(1232)$

$E_{1+}$ :  $P_{33}(1232)$

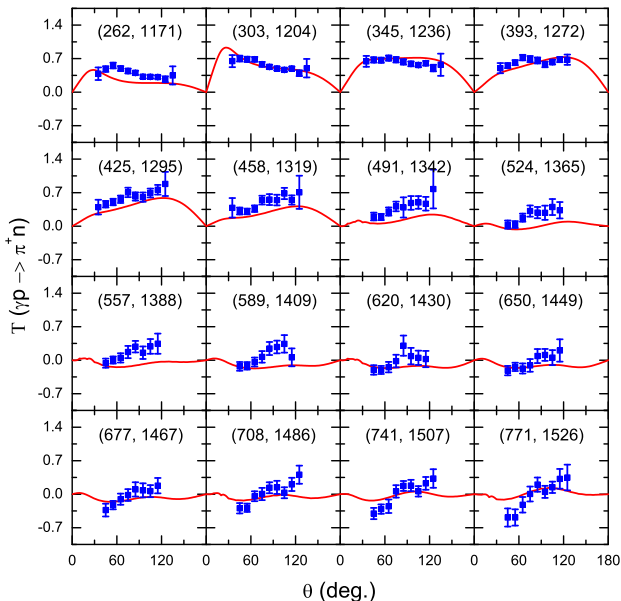
$M_{1-}$ :  $P_{31}(1910)$

- More data needed in the fit for further constraints





# Target asymmetries for $\gamma + p \rightarrow \pi^+ + n$



- Data are not included in the fit
- Good at low energies
- More partial waves needed  
 $J = 5/2: E_{2+}, M_{2+}$
- More channels needed  
 $\Delta K, \Sigma K, et al.$



# Summary & perspectives

- Jülich dynamical coupled-channels model
  - $\pi N \oplus \eta N \oplus \pi \Delta \oplus \rho N \oplus \sigma N$  (version 2002)
  - Wess & Zumino chiral Lagrangian +  $\Delta, \omega, \eta, a_0, \sigma$
  - $S_{11}(1535), S_{11}(1650), S_{31}(1620), P_{31}(1910), P_{13}(1720), D_{13}(1520), P_{33}(1232), D_{33}(1700)$
  - $\pi N \rightarrow \pi N$  scattering described successfully
- $\pi$  photoproduction
  - Field-theoretical approach
  - Gauge invariance strictly respected
  - $d\sigma/d\Omega$  &  $\Sigma_\gamma$  described well up to 1.65 GeV
  - Loop integral &  $M_c^\mu$  (apart from K.R.) are important
- Next step work:
  - Resonances' electromagnetic couplings
  - High spin resonances
  - $\Lambda K, \Sigma K$  &  $\omega N$  channels
  - Photoproduction of  $\eta, K, \omega$
  - Electroproduction



# Covariance & 3-D integral equation

- Jülich  $\pi N$  model — TOPT

$$T_{\text{TO}}(\mathbf{p}', \mathbf{p}; \sqrt{s}) = V_{\text{TO}}(\mathbf{p}', \mathbf{p}; \sqrt{s}) + \int d^3 p'' V_{\text{TO}}(\mathbf{p}', \mathbf{p}''; \sqrt{s}) G_{\text{TO}}(\mathbf{p}'', \sqrt{s}) T_{\text{TO}}(\mathbf{p}'', \mathbf{p}; \sqrt{s})$$

$$G_{\text{TO}}(\mathbf{p}'', \sqrt{s}) = \frac{1}{\sqrt{s} - E(\mathbf{p}'') - \omega(\mathbf{p}'') + i0}$$

- Converting to a covariant 3-D reduction like equation

$$V(\mathbf{p}', \mathbf{p}; \sqrt{s}) \equiv (2\pi)^3 \sqrt{2E(\mathbf{p}') 2\omega(\mathbf{p}')} \sqrt{2E(\mathbf{p}) 2\omega(\mathbf{p})} V_{\text{TO}}(\mathbf{p}', \mathbf{p}; \sqrt{s})$$

$$T(\mathbf{p}', \mathbf{p}; \sqrt{s}) \equiv (2\pi)^3 \sqrt{2E(\mathbf{p}') 2\omega(\mathbf{p}')} \sqrt{2E(\mathbf{p}) 2\omega(\mathbf{p})} T_{\text{TO}}(\mathbf{p}', \mathbf{p}; \sqrt{s})$$

$$T(\mathbf{p}', \mathbf{p}; \sqrt{s}) = V(\mathbf{p}', \mathbf{p}; \sqrt{s}) + \int \frac{d^3 p''}{(2\pi)^3} V(\mathbf{p}', \mathbf{p}''; \sqrt{s}) G_0(\mathbf{p}'', \sqrt{s}) T(\mathbf{p}'', \mathbf{p}; \sqrt{s})$$

$$G_0(\mathbf{p}'', \sqrt{s}) \equiv \frac{1}{2E(\mathbf{p}'') 2\omega(\mathbf{p}'')} \frac{1}{\sqrt{s} - E(\mathbf{p}'') - \omega(\mathbf{p}'') + i0}$$

- Similarly, make 3-D reduction of the covariant photoproduction equation